

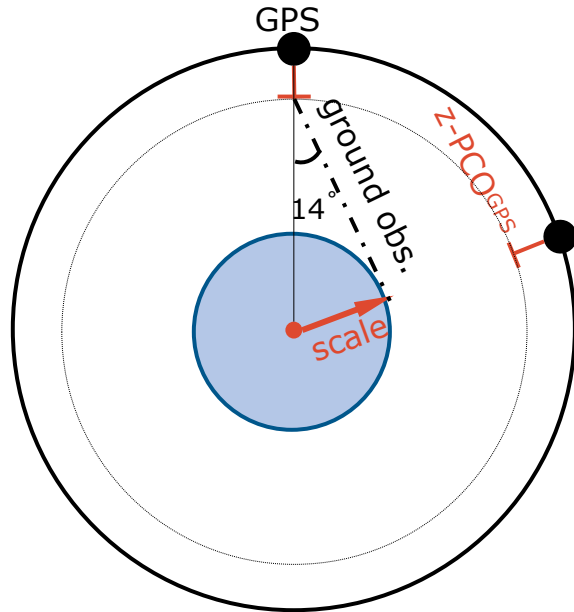
GNSS-based scale realization by integrating LEOs

Wen Huang¹, Benjamin Männel¹, Andreas Brack¹, Harald Schuh^{1,2}

1. Helmholtz Centre Potsdam, GFZ German Research Centre for Geosciences
2. Technische Universität Berlin, Institute of Geodesy and Geoinformation Science

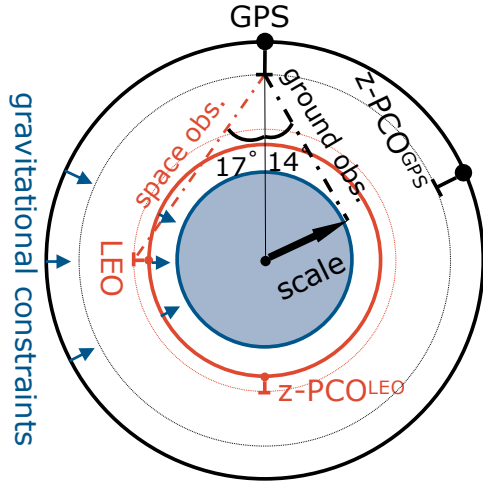


Can we derive a GNSS-based terrestrial scale?

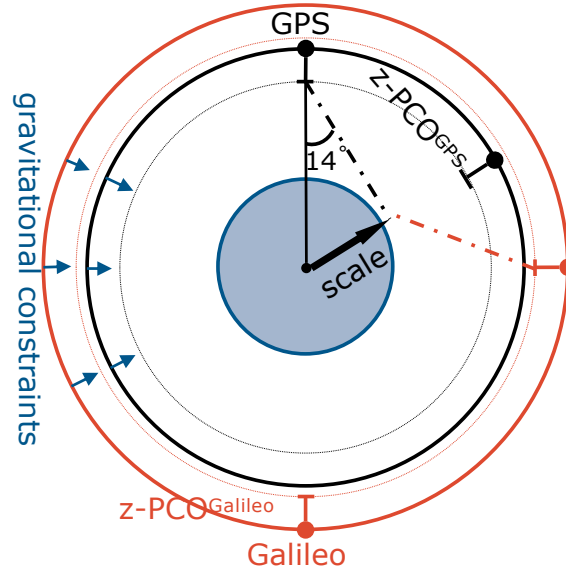


- Issues:
 - $z\text{-PCO}^{\text{GPS}}$ are highly correlated with the scale:
 - 13 cm $z\text{-PCO}^{\text{GPS}} \rightarrow 1$ ppb scale (Zhu et al. 2003)
 - 0.85 correlation coefficient (Huang et al. 2022)
 - $z\text{-PCO}^{\text{GPS}}$ given by the manufacturers were not convincing (Ge et al. 2005)
- Solution of the IGS:
 - estimating GNSS $z\text{-PCOs}$ by introducing scale determined by VLBI and SLR
 - ITRF scale is propagated to users and applications

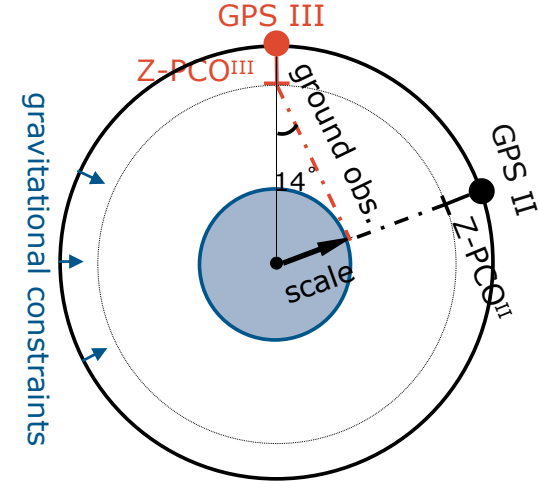
Three methods of solving the issue



LEOs-based



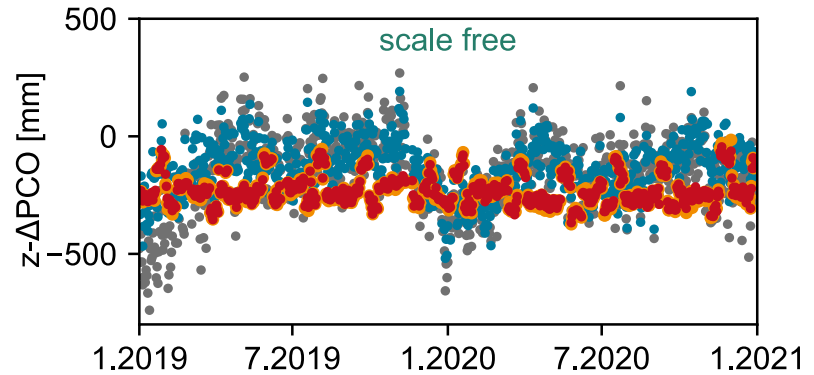
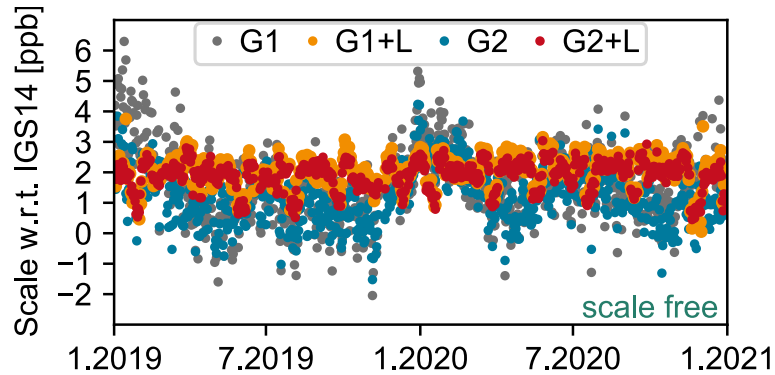
Galileo-based



GPS III-based

- properly calibrated z-PCOs (Sat./Rev.)
- Without no-net-scale (NNS) condition
- gravitational constrains (orb. dynamic)

Solutions of LEOs-based method



- G1 and G2: networks with different numbers of stations
- L: six LEOs (GRACE-FO, Jason-3, Swarm)
- scale free: NNS not applied

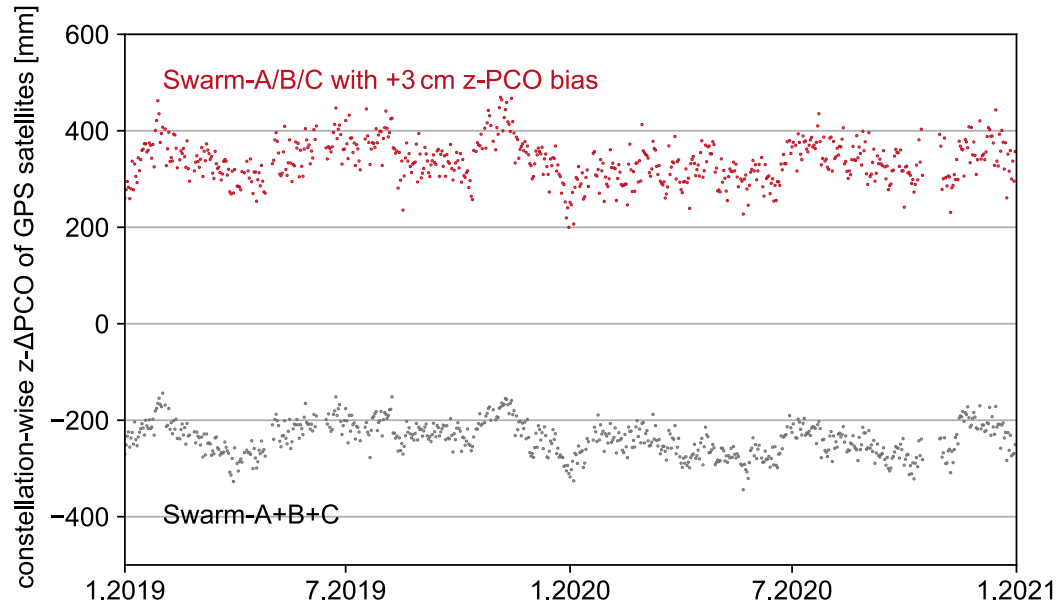
stations only → large variation
LEO-based → consistent
effective decorrelation

Solutions of subsets of the LEOs

subsets	LEOs	daily obs.	correlation	scale [ppb]	$\Delta\text{PCO}^{\text{GPS}}$ [mm]
GRACE-FO-1	1	1797	0.68	$+1.60 \pm 0.80$	-198 ± 85
GRACE-FO-2	1	1876	0.67	$+1.21 \pm 0.45$	-138 ± 52
Jason-3	1	2280	0.60	$+1.85 \pm 1.56$	-226 ± 228
Swarm-A	1	2091	0.64	$+1.85 \pm 0.40$	-225 ± 45
Swarm-B	1	2111	0.63	$+1.87 \pm 0.42$	-228 ± 47
GRACE-FO-1/2	2	3705	0.58	$+1.45 \pm 0.47$	-177 ± 47
Swarm-A/B/C	3	6282	0.46	$+1.95 \pm 0.32$	-238 ± 35
Swarm + G-FO	5	9987	0.39	$+1.83 \pm 0.30$	-223 ± 30
All LEOs	6	12275	0.32	$+1.86 \pm 0.64$	-228 ± 82

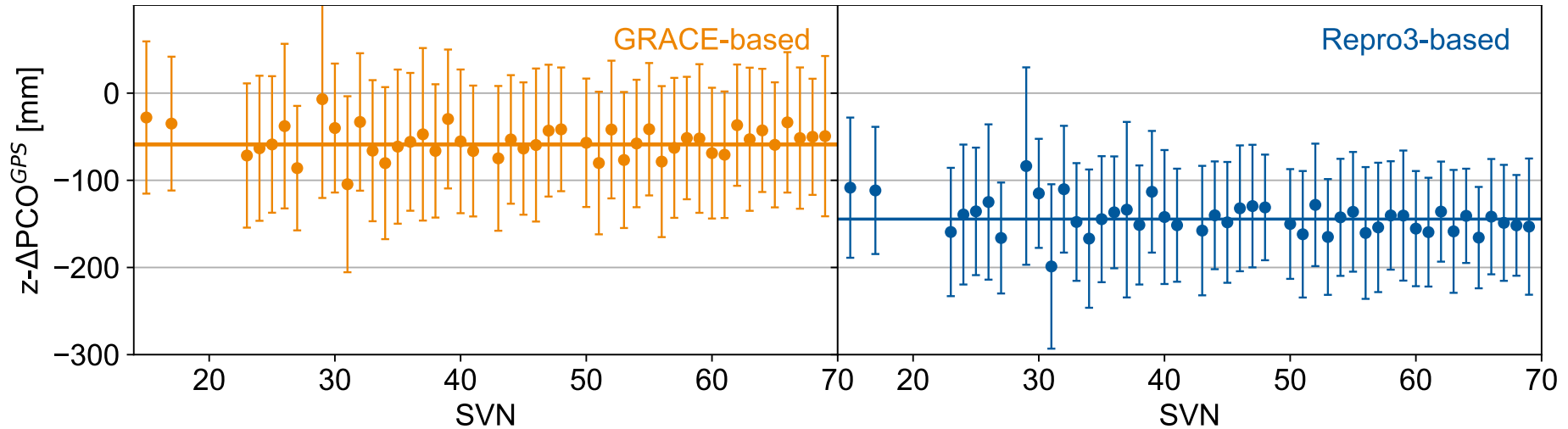
- better decorrelation
 - more LEOs
 - more onboard observations
- Agreement
- GRACE-FO results?
 - Post-launched z-PCO

Requirement on the z-PCOs of LEOs



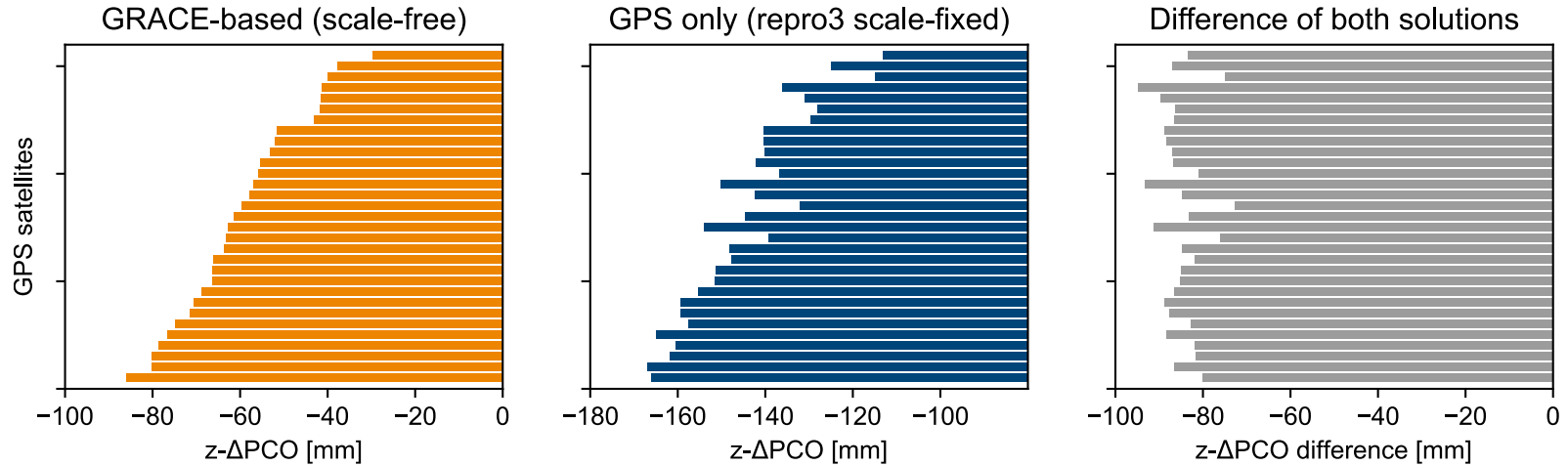
- +3 cm z-PCO of LEOs leads to:
 - -574 mm $z-\Delta\text{PCO}^{\text{GPS}}$
 - +4.27 ppb scale (+27mm)
- 1 mm accuracy of $z\text{-PCO}^{\text{LEO}}$ to achieve 1 mm scale
 - agrees with the simulation study by Glaser et al. (2020)

Solutions of 12-year processing: $z\text{-}\Delta\text{PCO}^{\text{GPS}}$



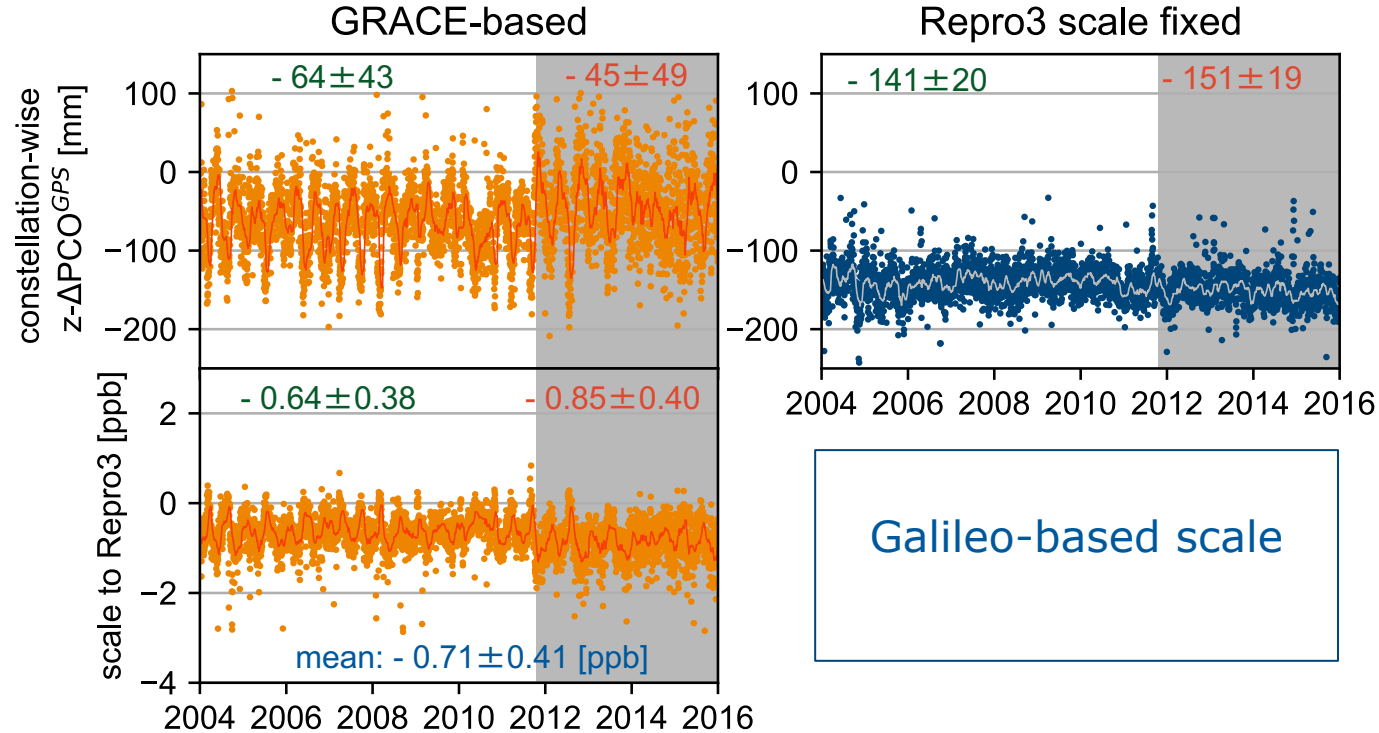
- 12-year processing
 - 2004-2015
 - GRACE-A/B (2 LEOs)
 - GPS (51 in total, 46 with 300+ days)
 - repro3 level 1&2 stations (100-130)
- compared to igs14.atx
- $z\text{-}\Delta\text{PCO}^{\text{GPS}}$
 - 85 mm difference in average
 - post-launched $z\text{-}\text{PCO}^{\text{GRACE}}$
 - Repro3-based 144 instead of 160 mm

Solutions of 12-year processing: $z\text{-}\Delta\text{PCO}^{\text{GPS}}$



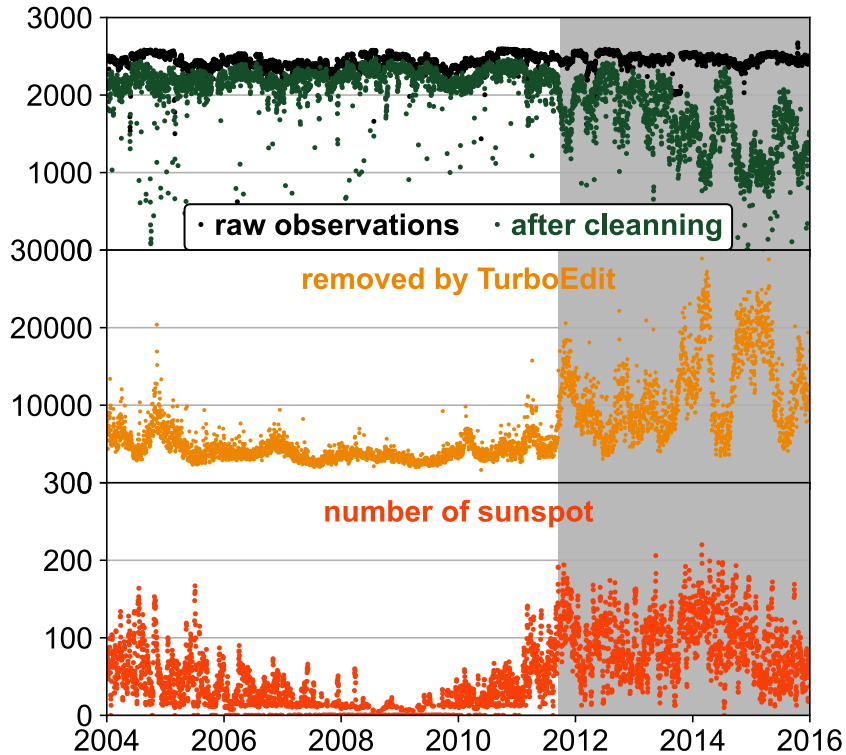
- sorted by $z\text{-}\text{PCO}^{\text{GPS}}$ corrections in GRACE-based solution
- agreement with an offset of 85 ± 5 mm
 - precise and reliable
 - not accurate due to post-launched $z\text{-}\text{PCO}^{\text{GRACE}}$
- satellite-specific corrections
 - 5 cm difference between satellites in maximum

Solutions of 12-year processing: time series



- consistent solution
 - annual signal
- steps start in 2011
 - in both solutions
 - different directions

Impact of solar activity

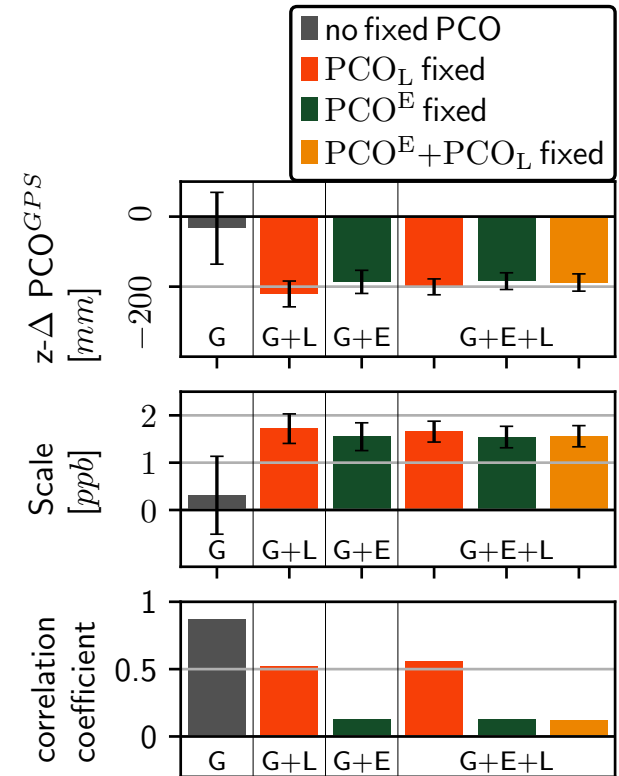


- reduced observation (after cleaning)
- newsletter of GRACE (2011.09&11)
 - degraded POD due to increased solar activity
 - re-optimized POD strategy
- more exclusion by TurboEdit
- highly related to solar activity
- further investigation needed
 - resolved by re-optimization?
 - step also in scale-fixed solution
 - first IOV of Galileo ? (2011.10)

Cross-check of LEO- and Galileo-based methods

- based on Galileo:
 - scale based on Galileo is propagated to GPS z-PCOs (Villiger et al. 2020)
 - GPS z-PCO: -160.0 mm
 - IGS repro3 derived a Galileo-based scale

- first validation of the two methods
- G: GPS (32); E: Galileo (24); L: Swarm (3)
- scale free: NNS not applied
- good agreement
- Galileo solution dominating due to the larger number of satellites (24 vs. 3)



Conclusions

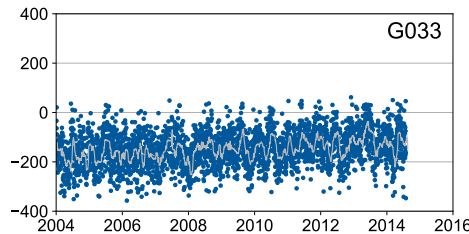
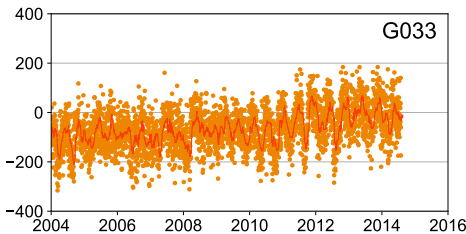
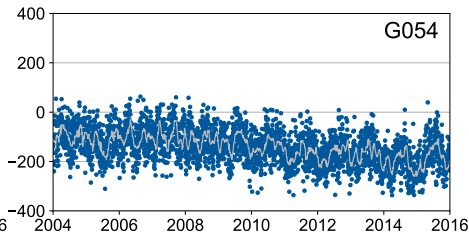
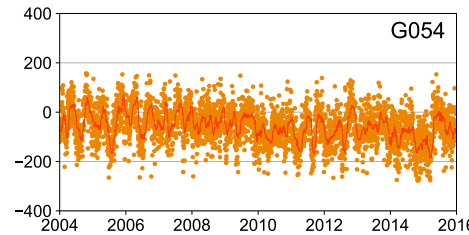
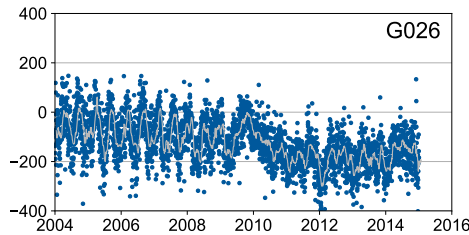
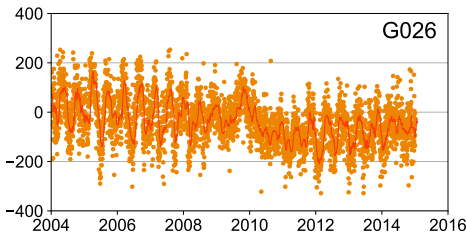
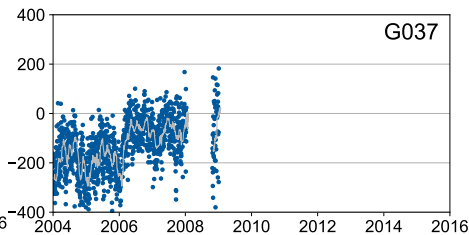
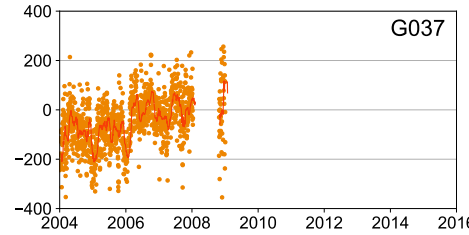
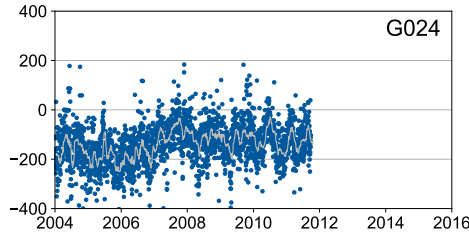
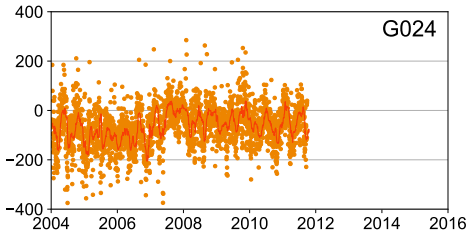
- The estimation $z\text{-PCO}^{\text{GPS}}$ and the realization of a pure GNSS-based scale is achieved by integrating LEOs.
- More LEOs and more onboard observations lead to better decorrelation of the two parameters.
- A 1-mm accuracy of the LEO $z\text{-PCOs}$ is required for the GGOS goal (1 mm scale).
- The LEO-based method has advantage in long-term study back in time. Satellite-specific $z\text{-PCO}^{\text{GPS}}$ corrections are proposed based on a 12-year study.
- Solar activity has impact on the GRACE observations.
- Further study is need to explain all the phenomenon in the long-term results.
- LEOs- and Galileo-based methods agree well with each other with slight difference.

References

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Thank you for your attention!

z- Δ PCO of Individual satellites



- trends
- stages